

diese A wegg:

$$A(4|1), B(2|0), C(4|-3), D(2|-6), E(-2|1)$$

$$\vec{BD} = \begin{pmatrix} 2 \\ -6 \end{pmatrix} - \begin{pmatrix} 2 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ -6 \end{pmatrix} \perp \begin{pmatrix} 6 \\ 0 \end{pmatrix} \rightarrow 6x = 12 \Rightarrow 6x - 12 = 0 \quad \left. \right\} f(x,y)$$

$$\vec{EC} = \begin{pmatrix} 4 \\ -3 \end{pmatrix} - \begin{pmatrix} -2 \\ 1 \end{pmatrix} = \begin{pmatrix} 6 \\ -4 \end{pmatrix} \perp \begin{pmatrix} 1 \\ 6 \end{pmatrix} \rightarrow x + 6y = -14 \Rightarrow x + 6y + 14 = 0 \quad \left. \right\} f(x,y)$$

$$\vec{BE} = \begin{pmatrix} -2 \\ 1 \end{pmatrix} - \begin{pmatrix} 2 \\ 0 \end{pmatrix} = \begin{pmatrix} -4 \\ 1 \end{pmatrix} \perp \begin{pmatrix} -2 \\ 4 \end{pmatrix} \rightarrow -2x + 4y = -2 \Rightarrow -2x + 4y + 2 = 0 \quad \left. \right\} g(x,y)$$

$$\vec{CD} = \begin{pmatrix} 2 \\ -6 \end{pmatrix} - \begin{pmatrix} -2 \\ 3 \end{pmatrix} = \begin{pmatrix} 4 \\ -9 \end{pmatrix} \perp \begin{pmatrix} -3 \\ 2 \end{pmatrix} \rightarrow -3x + 2y = -18 \Rightarrow -3x + 2y + 18 = 0 \quad \left. \right\} g(x,y)$$

$$f(x,y) : (6x - 12) \cdot (x + 6y + 14) = 0 \quad \left. \right\} \text{für } B, C, D \& E$$

$$g(x,y) : (-2x + 4y + 2) \cdot (-3x + 2y + 18) = 0$$

$$\lambda \cdot f(x,y) + \mu \cdot g(x,y) = 0 \quad \rightarrow \text{für } B, C, D \& E$$

$$\text{wähle } \lambda = \underbrace{g(x_A, y_A)}_{\text{"g(A)"}} \quad \wedge \quad \mu = -\underbrace{f(x_A, y_A)}_{\text{"-f(A)"}}$$

A in g, -f)

$$\lambda : g(A) : (-2 \cdot 4 + 4 \cdot (-1) + 2) \cdot (-3 \cdot 4 + 2 \cdot (-1) + 18) = 0$$

$$8 \cdot (-4) = (-8) \cdot 4 \rightarrow 32 = \underline{16 \cdot 2}$$

$$\mu : -f(A) : -[(6 \cdot 4 - 12) \cdot (4 + 6 \cdot (-1) + 14)] = 0$$

$$12 \cdot 12 = 144 < 16 \cdot 9$$

$$2 \cdot f(x,y) + 9 \cdot g(x,y) = 0$$

$$\begin{aligned} k : & 2 \zeta_{xx}^2 + 144 \zeta_{xy} + 336x - 48x - 288y - 672 - 6186x^2 - 324xy - 2916x \\ & - 972xy + 648y^2 + 5832y - 972x + 648y + 5832 \end{aligned}$$

$$\boxed{k : 11x^2 - 12xy + 72y^2 - 118x + 96y + 52 = 0}$$

